## Trees From Files

In Lab 5 (and in the last question on Prelab 5) there is an algorithm for reading a tree from a data file. The nodes are presented in the order of a postorder traversal of the tree. Each line of the data file has the form
data bit bit
where the first bit is 1 if the node has a left child and the second bit is 1 if the node has a right child.

For example
A 10
means that a node has data "A"; it has a left child but not a right child.

The algorithm for turning a file consisting of such lines into a tree makes use of a stack of trees. At each step:

1. Get the next line of the file and separate into its data, left-bit and right-bit components.
2. Build a new node for the line and insert the data into it.
3. If the right-bit is 1 pop the stack for the node's right child.
4. If the left-bit is 1 pop the stack for the node's left child.
5. Push the node onto the stack

When you reach the end of the file there should be 1 item on the stack --- the entire tree.

For example: D 00 E 00
C 11
B 01
G 00
H 00
F 11
A 11

We read the first two lines: $D$ and $E$ have no children so the singleton nodes are pushed onto the stack with E on top of D. Node C has two children so node C pops E as its right child, D as its left:


This node is pushed onto the stack; we'll call it treeC.

| D 00 | We next read line B 01. |
| :--- | :--- |
| E 00 | We make a node with data B and |
| C 11 | pop treeC off the stack as B's |
| B 01 | right child: |
| G 00 |  |
| H 00 |  |
| F 11 |  |
| A 11 |  |

We'll call this treeB. It gets pushed onto the stack.

| D | 0 | 0 |
| :--- | :--- | :--- |
| E | 0 | 0 |
| C | 1 | 1 |
| B | 0 | 1 |
| G | 0 | 0 |
| H | 0 | 0 |
| F | 1 | 1 |
| A | 1 | 1 |

Next nodes G and H are made as trees with no children and are pushed onto the stack. The stack is now

$$
\begin{aligned}
& \text { node } \mathrm{H} \\
& \text { node G } \\
& \text { treeB }
\end{aligned}
$$

The next line of the file builds treeF with H as its right child and G as its left:


| D | 0 | 0 |
| :--- | :--- | :--- |
| E | 0 | 0 |
| C | 1 | 1 |
| B | 1 | 1 |
| G | 0 | 0 |
| H | 0 | 0 |
| F | 1 | 1 |
| A | 1 | 1 |

TreeF is pushed onto the stack above treeB. The last line of the file tells us to build a new node A. We pop treeF as its right child and treeB as its left:


